Communication Performance in Network-on-Chips

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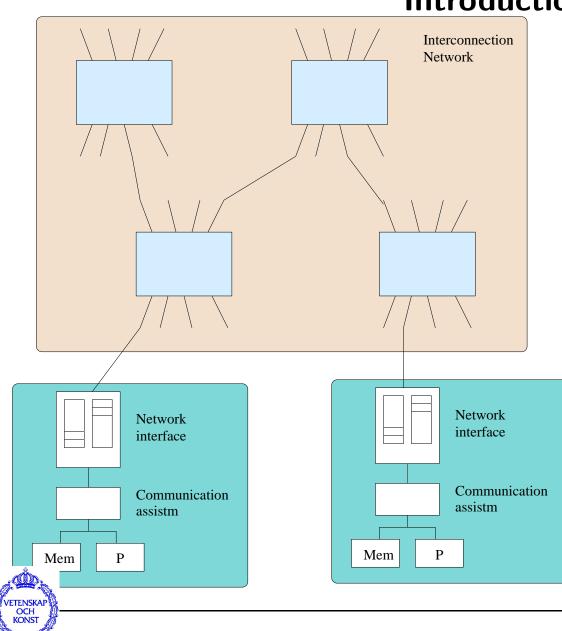
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Overview

Introduction **Communication** Performance **Organizational Structure** Interconnection Topologies Trade-offs in Network Topology Routing Switch Design Flow Control **NoC Examples**





Introduction

- **Topology**: How switches and nodes are connected
- Routing algorithm: determines the route from source to destination
- Switching strategy: how a message traverses the route
- Flow control: Schedules the traversal of the message over time



Message is the basic communication entity.



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Direct network is a network where each switch connects to a node.

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Routing distance between two nodes is the number of hops

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Average distance is the average of the routing distance over all pairs of nodes.



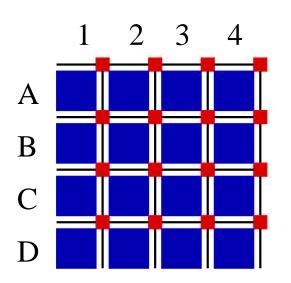
Basic Switching Techniques

Circuit Switching A real or virtual circuit establishes a direct connection between source and destination.

- **Packet Switching** Each packet of a message is routed independently. The destination address has to be provided with each packet.
- **Store and Forward Packet Switching** The entire packet is stored and then forwarded at each switch.
- **Cut Through Packet Switching** The flits of a packet are pipelined through the network. The packet is not completely buffered in each switch.
- Virtual Cut Through Packet Switching The entire packet is stored in a switch only when the header flit is blocked due to congestion.
- **Wormhole Switching** is cut through switching and all flits are blocked on the spot when the header flit is blocked.



Latency



Time(n) = Admission + ChannelOccupancy + RoutingDelay + ContentionDelay

Admission is the time it takes to emit the message into the network.

ChannelOccupancy is the time a channel is occupied.

RoutingDelay is the delay for the route.



ContentionDelay is the delay of a message due to contention.

Channel Occupancy

ChannelOccupancy
$$= \frac{n + n_E}{b}$$

 $n \dots$ message size in bits $n_E \dots$ envelop size in bits $b \dots$ raw bandwidth of the channel



Routing Delay

Store and Forward:

Circuit Switching:

Store and Forward with fragmented packets:

Cut Through:

 $T_{sf}(n,h) = h(\frac{n}{b} + \Delta)$

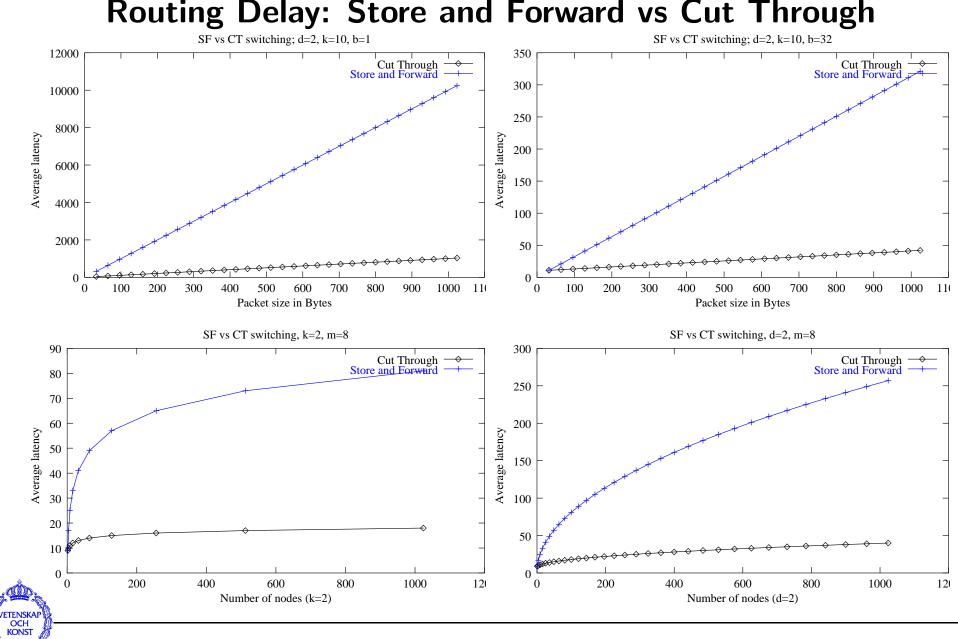
$$T_{cs}(n,h) = \frac{n}{b} + h\Delta$$

$$T_{cs}(n,h,n_p) = \frac{n-n_p}{b} + h(\frac{n_p}{b} + \Delta)$$

$$T_{ct}(n,h) = \frac{n}{b} + h\Delta$$

 $n \dots$ message size in bits $n_p \dots$ size of message fragments in bits $h \dots$ number of hops $b \dots$ raw bandwidth of the channel $\Delta \dots$ switching delay per hop





Routing Delay: Store and Forward vs Cut Through

Local and Global Bandwidth

Local bandwidth = $b\left(\frac{n}{n+n_E+w\Delta}\right)$ **Bisection bandwidth**

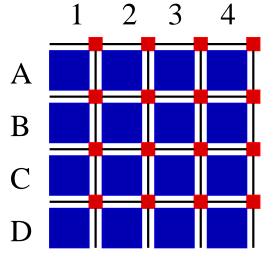
Total bandwidth = Cb[bits/second] = Cw[bits/cycle] = C[phits/cycle]... minimum bandwidth to cut the net into two equal parts.

b ... raw bandwidth of a link; $n \dots$ message size; n_E ... size of message envelope; $w \dots$ link bandwidth per cycle;

- Δ ... switching time for each switch in cycles;
- $w\Delta$... bandwidth lost during switching;
- C ... total number of channels;

For a $k \times k$ mesh with bidirectional channels:

Total bandwidth = $(4k^2 - 4k)b$ Bisection bandwidth = 2kb





Link and Network Utilization

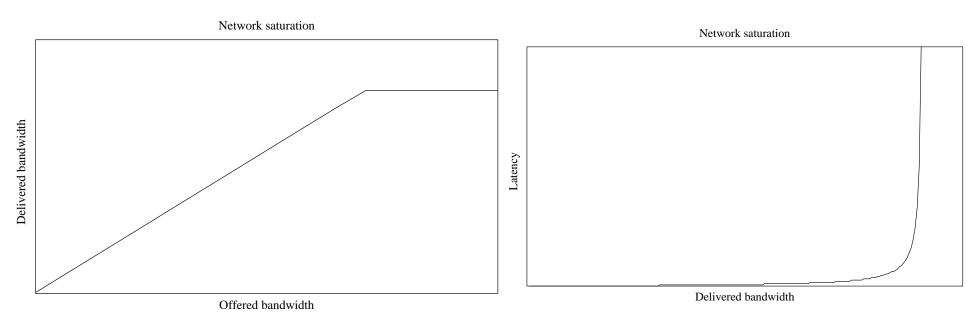
total load on the network:
$$L = \frac{Nhl}{M}$$
[phits/cycle]

load per channel:
$$\rho = \frac{Nhl}{MC}$$
[phits/cycle] ≤ 1

M ... each host issues a packet every M cycles C ... number of channels N ... number of nodes h ... average routing distance l = n/w ... number of cycles a message occupies a channel n ... average message size w ... bitwidth per channel



Network Saturation



Typical saturation points are between 40% and 70%. The saturation point depends on

- Traffic pattern
- Stochastic variations in traffic
- Routing algorithm



Organizational Structure

- Link
- Switch
- Network Interface

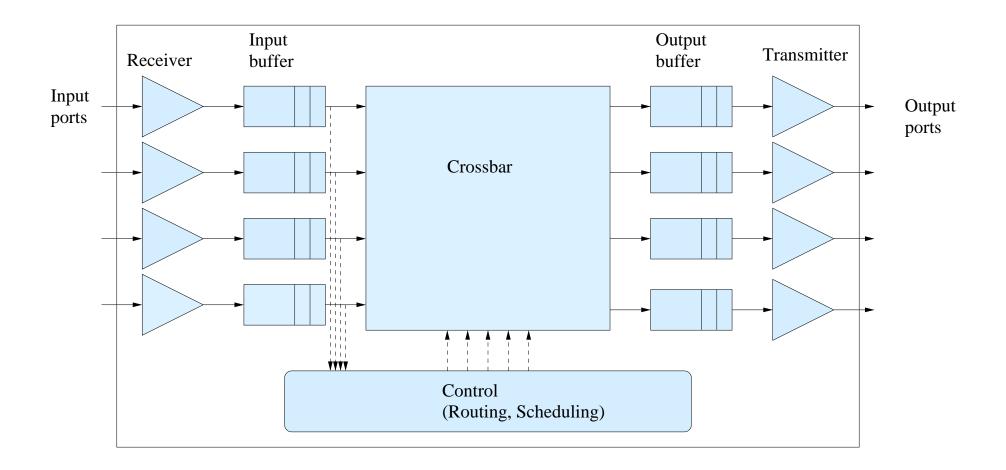


Link

- **Short link** At any time there is only one data word on the link.
- **Long link** Several data words can travel on the link simultaneously.
- **Narrow link** Data and control information is multiplexed on the same wires.
- Wide link Data and control information is transmitted in parallel and simultaneously.
- **Synchronous clocking** Both source and destination operate on the same clock.
- **Asynchronous clocking** The clock is encoded in the transmitted data to allow the receiver to sample at the right time instance.



Switch





Switch Design Issues

Degree: number of inputs and outputs;

Buffering

- Input buffers
- Output buffers
- Shared buffers

Routing

- Source routing
- Deterministic routing
- Adaptive routing

Output scheduling

Deadlock handling

Control flow



Network Interface

- Admission protocol
- Reception obligations
- Buffering
- Assembling and disassembling of messages
- Routing
- Higher level services and protocols

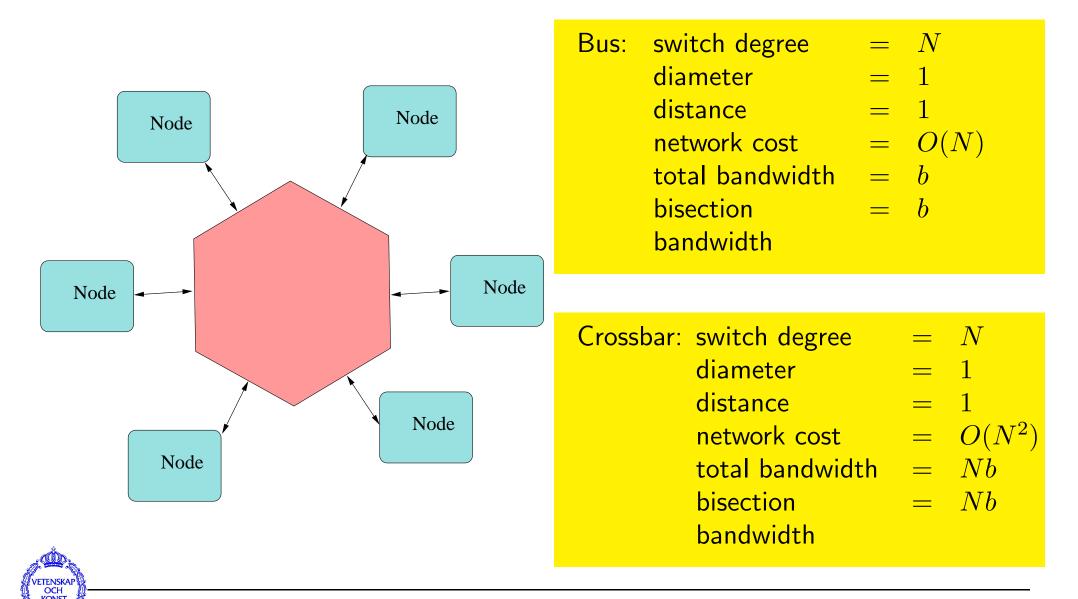


Interconnection Topologies

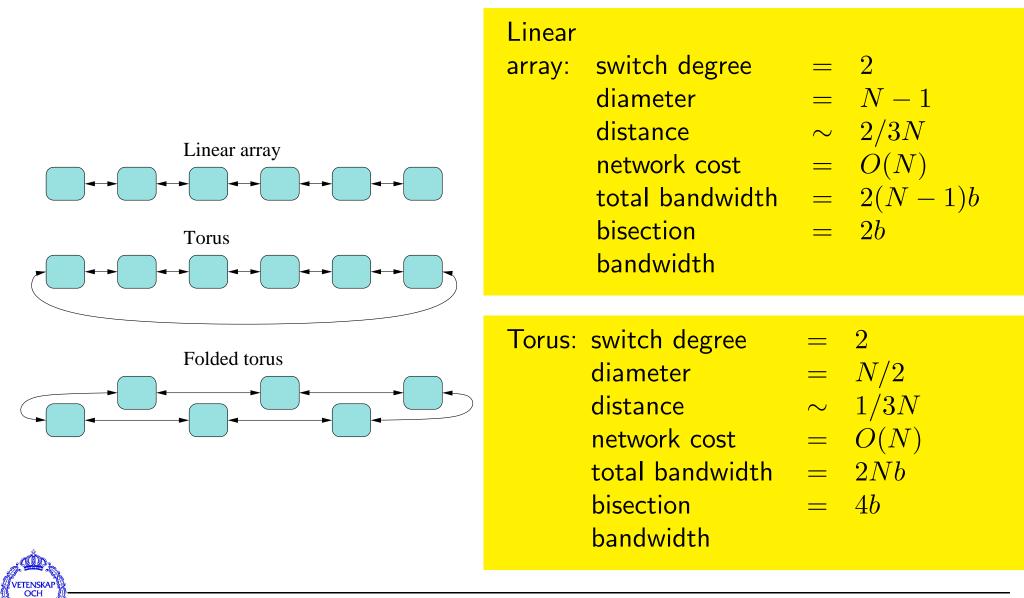
- Fully connected networks
- Linear arrays and rings
- Multidimensional meshes and tori
- Trees
- Butterflies



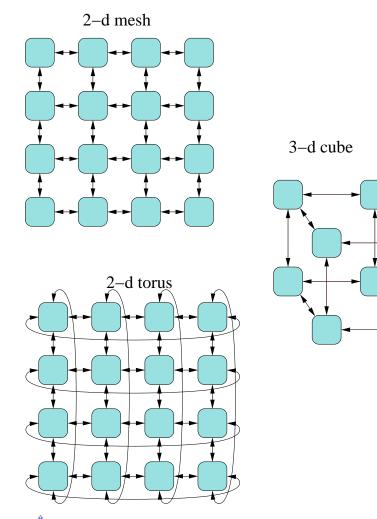
Fully Connected Networks



Linear Arrays and Rings



Multidimensional Meshes and Tori

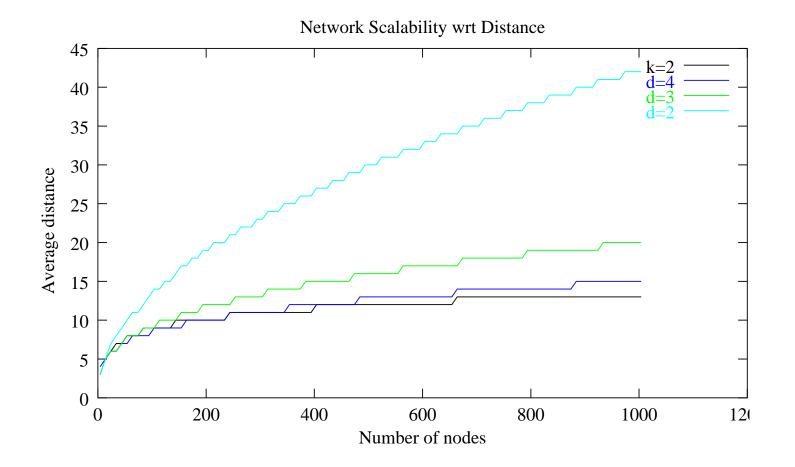


k-ary d-cubes are d-dimensional tori with unidirectional links and k nodes in each dimension:

=	k^d
=	d
=	d(k-1)
\sim	$d\frac{1}{2}(k-1)$
=	O(N)
=	2Nb
=	$2k^{(d-1)}b$
	>

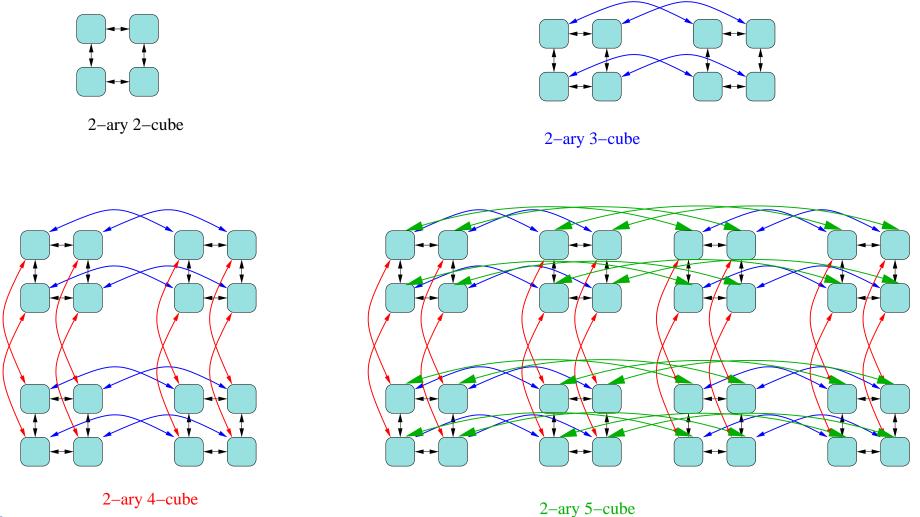


Routing Distance in *k*-ary *n*-Cubes



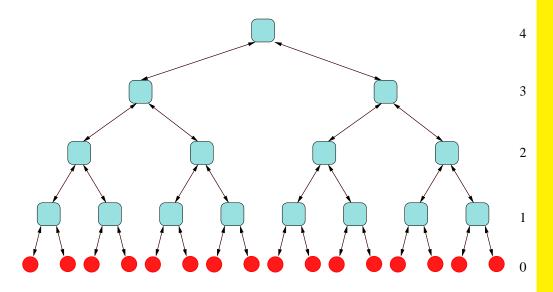


Projecting High Dimensional Cubes





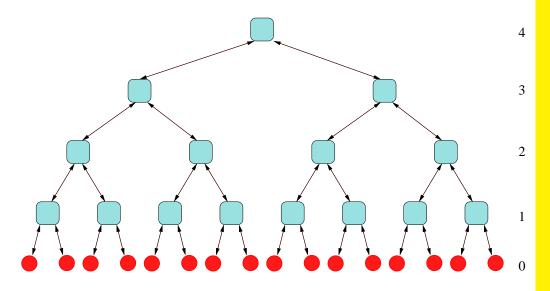
Binary Trees



number of nodes N	=	2^d
number of switches	—	$2^{d} - 1$
switch degree	=	3
diameter	=	2d
distance	\sim	d+2
network cost	—	O(N)
total bandwidth	—	$2 \cdot 2(N-1)b$
bisection bandwidth	=	2b



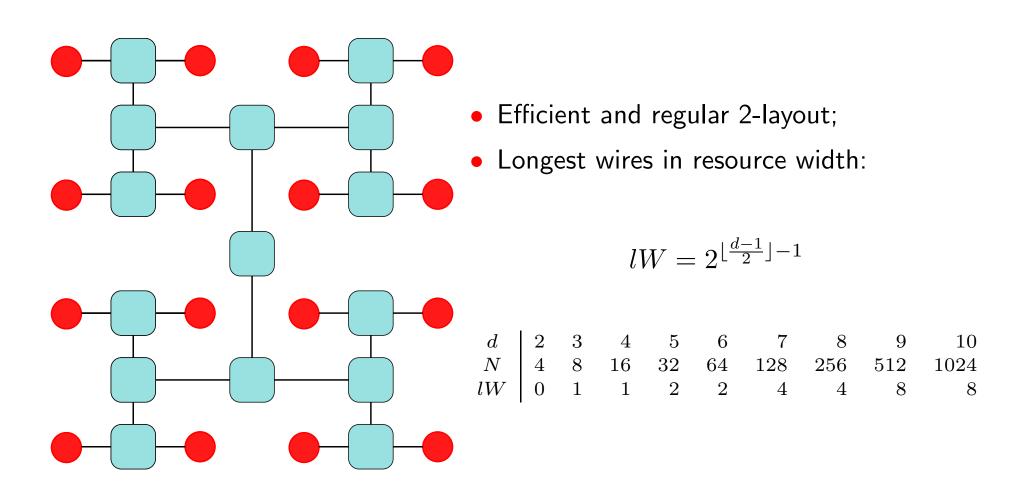
k-ary Trees



number of nodes N	=	k^d
number of switches	\sim	k^d
switch degree	=	k+1
diameter	=	2d
distance	\sim	d+2
network cost	=	O(N)
total bandwidth	=	$2 \cdot 2(N-1)b$
bisection bandwidth	=	kb



Binary Tree Projection





k-ary *n*-Cubes versus *k*-ary Trees

k-ary n-cubes:

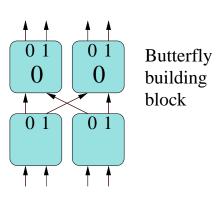
number of nodes N	=	k^d
switch degree	=	d+2
diameter	=	d(k-1)
distance	\sim	$d\frac{1}{2}(k-1)$
network cost	=	O(N)
total bandwidth	=	2Nb
bisection bandwidth	=	$2k^{(d-1)}b$

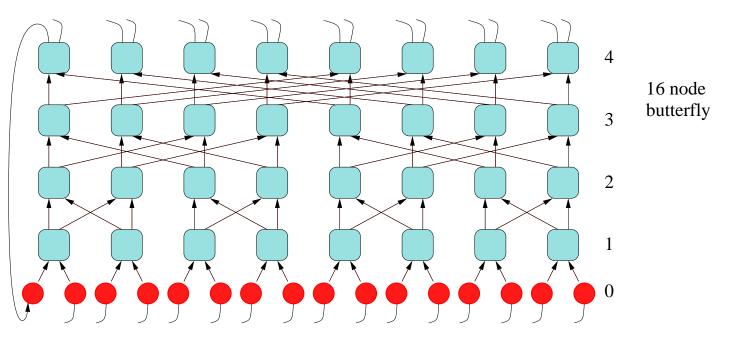
k-ary trees:

number of nodes N	=	k^d
number of switches	\sim	k^d
switch degree	=	k+1
diameter	=	2d
distance	\sim	d+2
network cost	=	O(N)
total bandwidth	=	$2 \cdot 2(N-1)b$
bisection bandwidth	=	kb



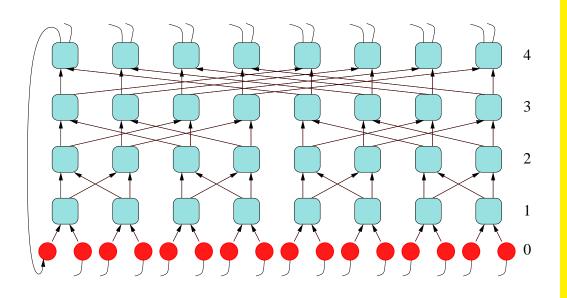
Butterflies







Butterfly Characteristics



=	2^d
=	$2^{d-1}d$
=	2
=	d+1
_	d+1
=	O(Nd)
=	$2^d db$
=	$\frac{N}{2}b$
	=



k-ary *n*-Cubes versus *k*-ary Trees vs Butterflies

	k-ary n -cubes	binary tree	butterfly
cost per node	O(N)	O(N)	$O(N \log N)$
distance	$\frac{1}{2}\sqrt[d]{N}\log N$	$2\log N$	$\log N$
links per node	2	2	$\log N$
bisection	$2N^{\frac{d-1}{d}}$	1	$rac{1}{2}N$
frequency limit of random traffic	$\sqrt[d]{\frac{N}{2}}$	N	2

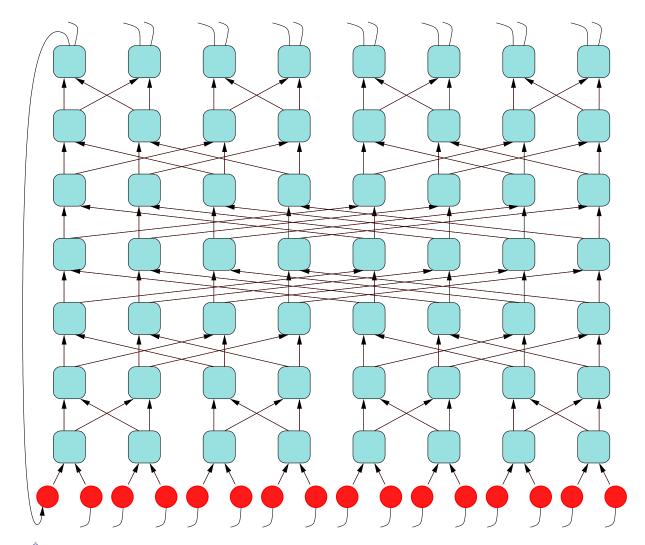


- Cost of the network
 - $\star O(N \log N)$
 - ★ 2-d layout is more difficult than for binary trees
 - ★ Number of long wires grows faster than for trees.
- For each source-destination pair there is only one route.
- Each route blocks many other routes.



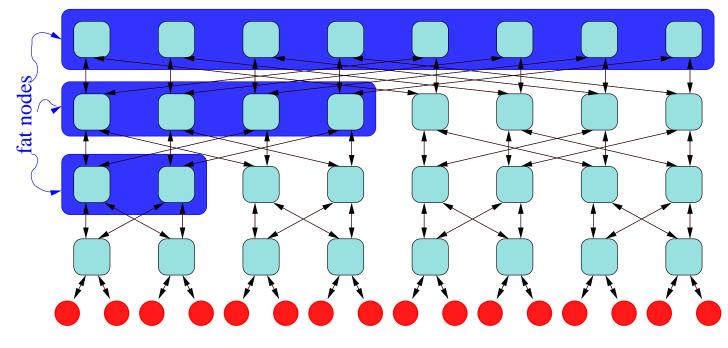
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- Many routes;
- Costly to compute non-blocking routes;
- High probability for non-blocking route by randomly selecting an intermediate node [Leighton, 1992];

Fat Trees

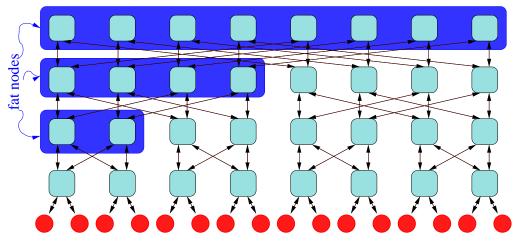


16-node 2-ary fat-tree



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k-ary *n*-dimensional Fat Tree Characteristics



16-node 2-ary fat-tree

number of nodes N	=	k^d
number of switches	=	$k^{d-1}d$
switch degree	=	2k
diameter	=	2d
distance	\sim	d
network cost	=	O(Nd)
total bandwidth	=	$2k^ddb$
bisection bandwidth	=	$2k^{d-1}b$



k-ary *n*-Cubes versus *k*-ary *d*-dimensional Fat Trees

k-ary *n*-cubes:

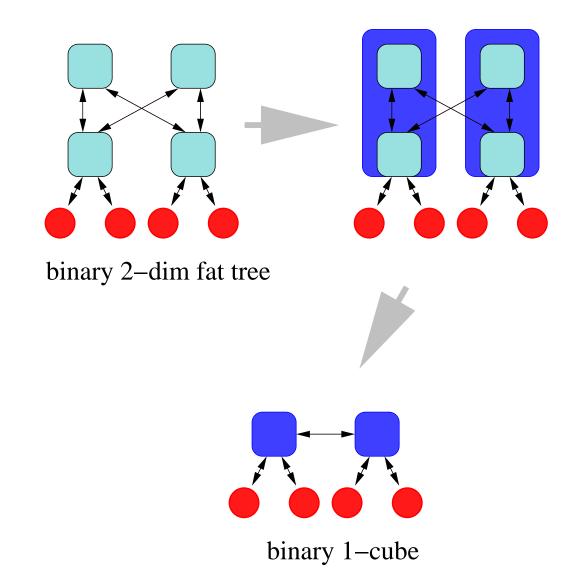
number of nodes N	=	k^d
switch degree	=	d
diameter	=	d(k-1)
distance	\sim	$d\frac{1}{2}(k-1)$
network cost	=	O(N)
total bandwidth	=	2Nb
bisection bandwidth	=	$2k^{(d-1)}b$

k-ary *n*-dimensional fat trees:

number of nodes N	=	k^d
number of switches	=	$k^{d-1}d$
switch degree	=	2k
diameter	=	2d
distance	\sim	d
network cost	=	O(Nd)
total bandwidth	=	$2k^ddb$
bisection bandwidth	=	$2k^{d-1}b$

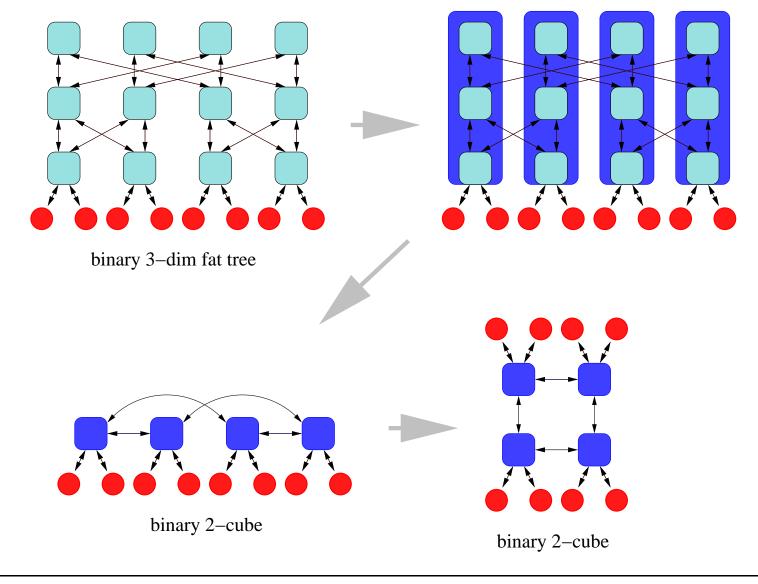


Relation between Fat Tree and Hypercube

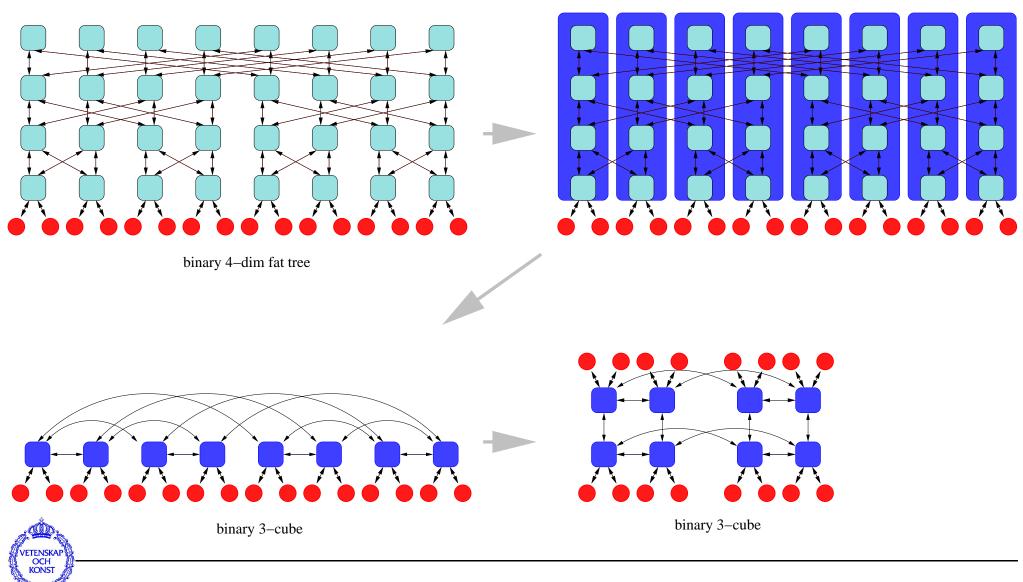




Relation between Fat Tree and Hypercube - cont'd



Relation between Fat Tree and Hypercube - cont'd



Topologies of Parallel Computers

Machine	Topology	Cycle Time [ns]	Channel width [bits]	Routing delay [cycles]	Flit size [bits]
nCUBE/2	Hypercube	25	1	40	32
TMC CM-5	Fat tree	25	4	10	4
IBM SP-2	Banyan	25	8	5	16
Intel Paragon	2D Mesh	11.5	16	2	16
Meiko CS-2	Fat tree	20	8	7	8
Cray T3D	3D Torus	6.67	16	2	16
DASH	Torus	30	16	2	16
J-Machine	3D Mesh	31	8	2	8
Monsoon	Butterfly	20	16	2	16
SGI Origin	Hypercube	2.5	20	16	160
Myricom	Arbitrary	6.25	16	50	16

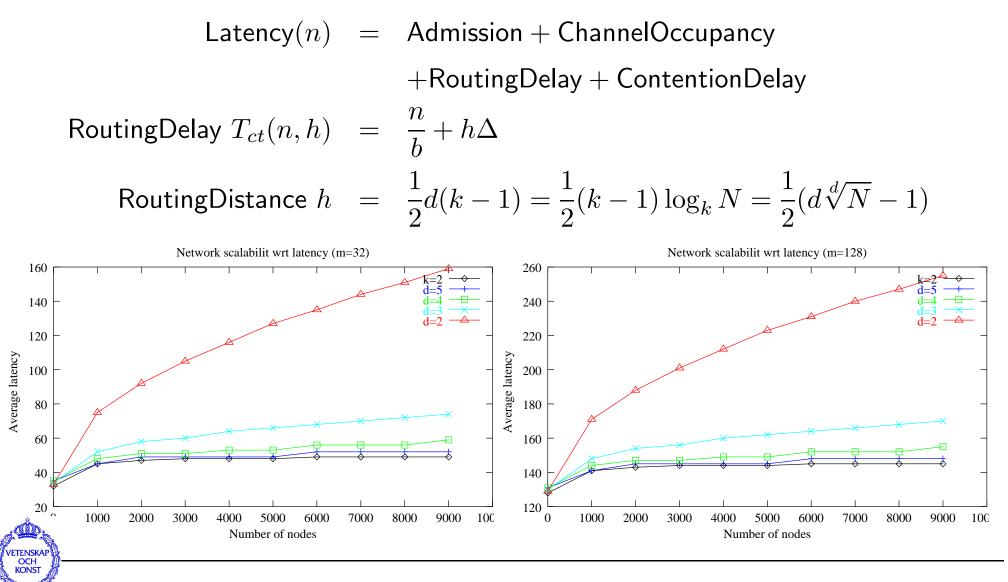


Trade-offs in Topology Design for the *k***-ary** *n***-Cube**

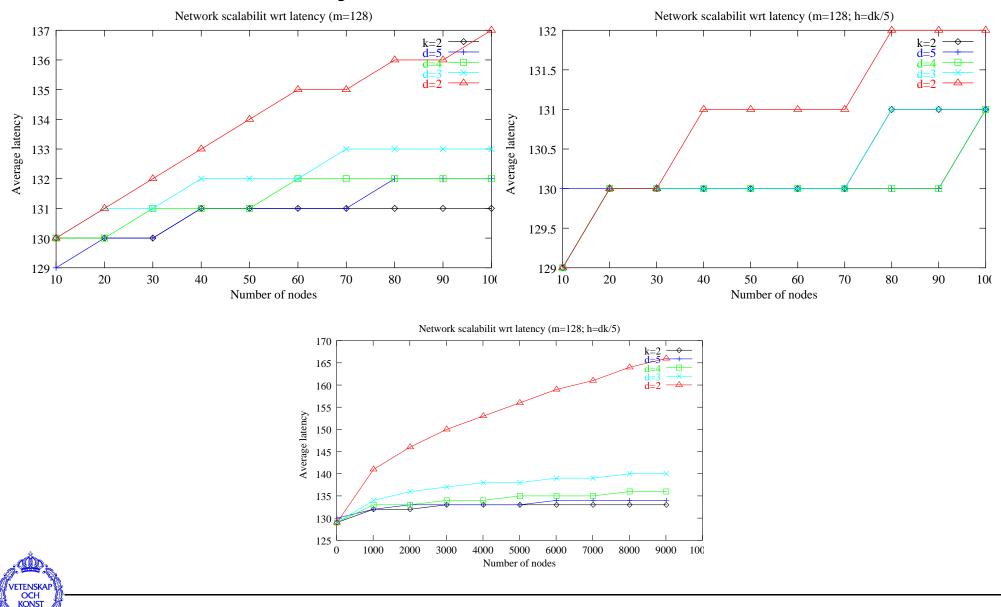
- Unloaded Latency
- Latency under Load



Network Scaling for Unloaded Latency

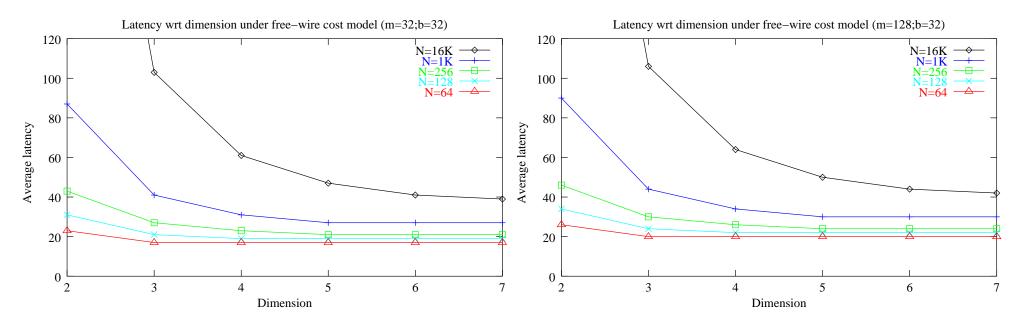


Unloaded Latency for Small Networks and Local Traffic



Unloaded Latency under a Free-Wire Cost Model

Free-wire cost model: Wires are free and can be added without penalty.

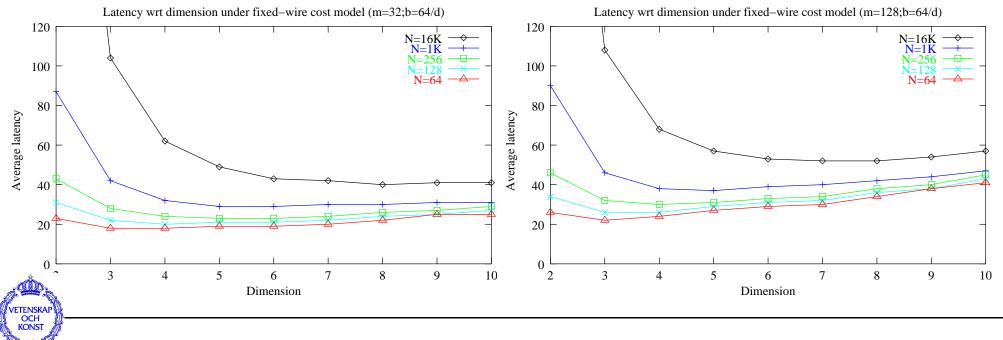




Unloaded Latency under a Fixed-Wire Cost Models

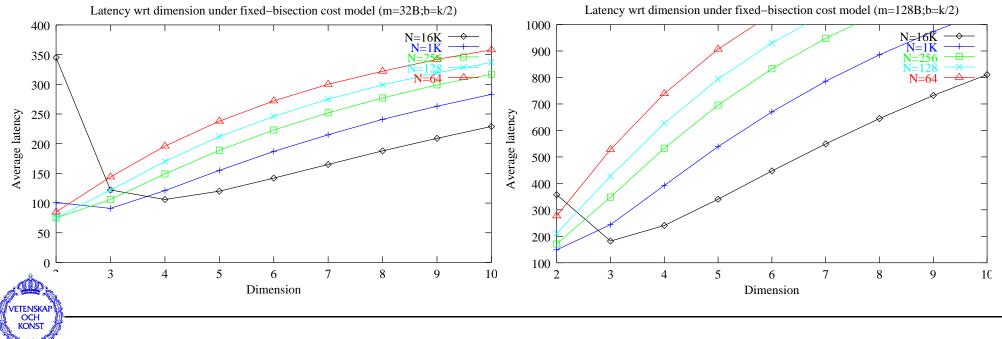
Fixed-wire cost model: The number of wires is constant per node:

128 wires per node: $w(d) = \lfloor \frac{64}{d} \rfloor$.



Unloaded Latency under a Fixed-Bisection Cost Models

Fixed-bisection cost model: The number of wires across the bisection is constant: bisection = 1024 wires: $w(d) = \frac{k}{2} = \frac{\sqrt[d]{N}}{2}$. Example: N=1024:

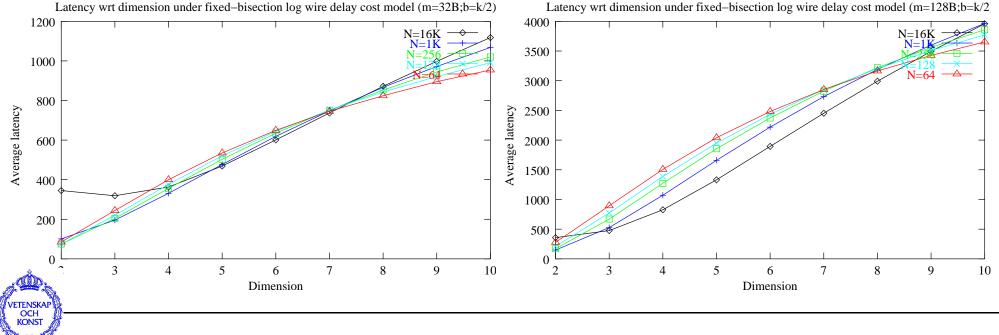


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Unloaded Latency under a Logarithmic Wire Delay Cost Models

Fixed-bisection Logarithmic Wire Delay cost model: The number of wires across the bisection is constant and the delay on wires increases logarithmically with the length [Dally, 1990]: Length of long wires: $l = k^{\frac{n}{2}-1}$

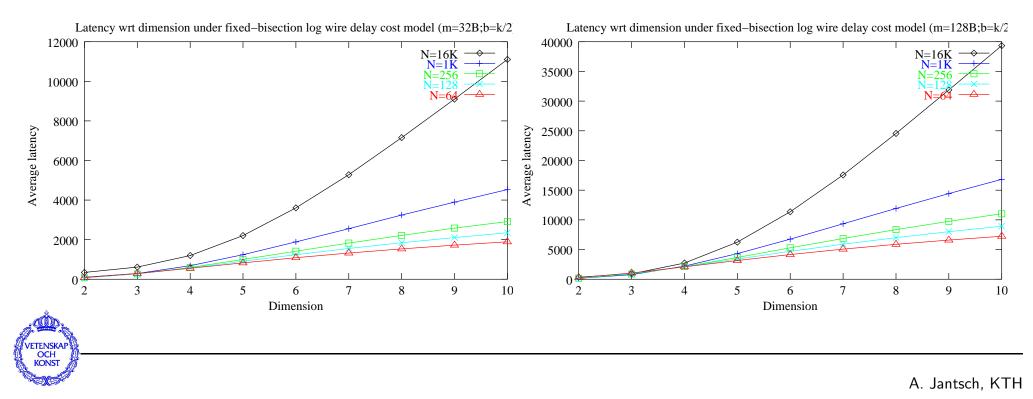
$$T_c \propto 1 + \log l = 1 + (\frac{d}{2} - 1) \log k$$



Unloaded Latency under a Linear Wire Delay Cost Models

Fixed-bisection Linear Wire Delay cost model: The number of wires across the bisection is constant and the delay on wires increases linearly with the length [Dally, 1990]: Length of long wires: $l = k^{\frac{n}{2}-1}$

$$T_c \propto l = k^{\frac{d}{2}-1}$$



Latency under Load

Assumptions [Agarwal, 1991]:

- *k*-ary *n*-cubes
- random traffic
- dimension-order cut-through routing
- unbounded internal buffers (to ignore flow control and deadlock issues)



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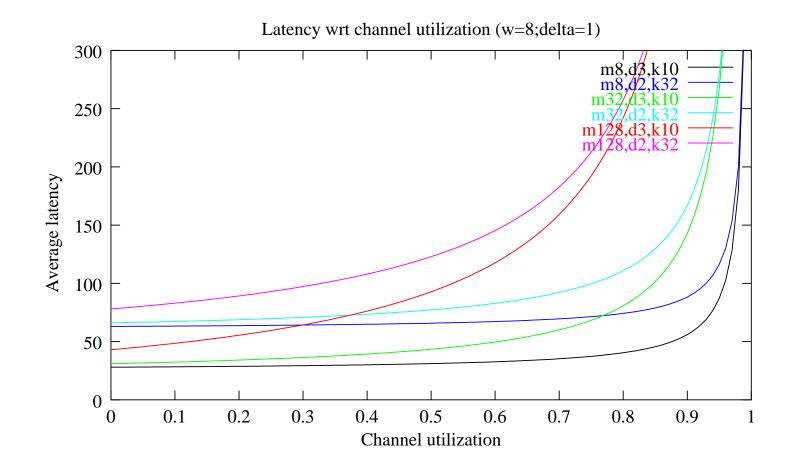
Latency under Load - cont'd

 $\mathsf{Latency}(n) = \mathsf{Admission} + \mathsf{ChannelOccupancy} + \mathsf{RoutingDelay} + \mathsf{ContentionDelay}$

$$\begin{split} T(m,k,d,w,\rho) &= \operatorname{RoutingDelay} + \operatorname{ContentionDelay} \\ T(m,k,d,w,\rho) &= \frac{m}{w} + dh_k (\Delta + W(m,k,d,w,\rho)) \\ W(m,k,d,w,\rho) &= \frac{m}{w} \cdot \frac{\rho}{(1-\rho)} \cdot \frac{h_k - 1}{h_k^2} \cdot \left(1 + \frac{1}{d}\right) \\ h &= \frac{1}{2} d(k-1) \end{split}$$

- $m \cdots$ message size
- $w \ \cdots$ bitwidth of link
- $\rho ~ \cdots$ aggregate channel utilization
- $h_k \cdots$ average distance in each dimension
- $\Delta \ \cdots$ switching time in cycles

Latency vs Channel Load





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Routing

Deterministic routing The route is determined solely by source and destination locations.

Arithmetic routing The destination address of the incoming packet is compared with the address of the switch and the packet is routed accordingly. (relative or absolute addresses)

Source based routing The source determines the route and builds a header with one directive for each switch. The switches strip off the top directive.

Table-driven routing Switches have routing tables, which can be configured.

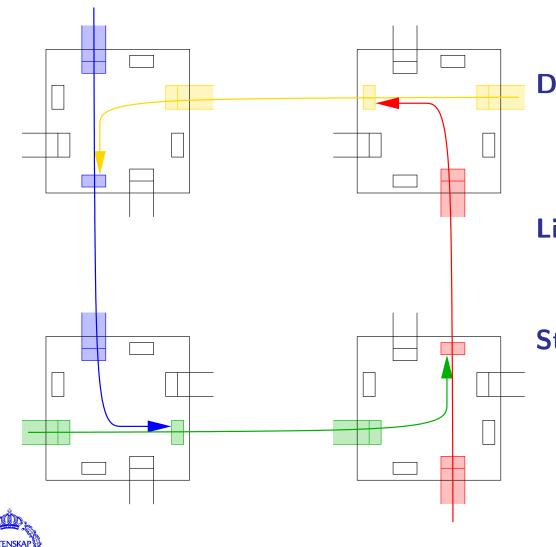
Adaptive routing The route can be adapted by the switches to balance the load.

Minimal routing allows only shortest paths while non-minimal routing allows even longer paths.



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Deadlock



Deadlock Two or several packets mutually block each other and wait for resources, which can never be free.

Livelock A packet keeps moving through the network but never reaches its destination.

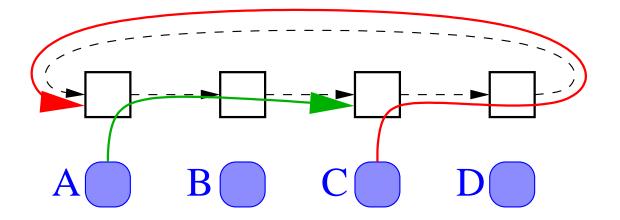
Starvation A packet never gets a resource because it always looses the competition for that resource (fairness).

Deadlock Situations

- Head-on deadlock;
- Nodes stop receiving packets;
- Contention for switch buffers can occur with store-and-forward, virtual-cut-through and wormhole routing. Wormhole routing is particularly sensible.
- Cannot occur in butterflies;
- Cannot occur in trees or fat trees if upward and downward channels are independent;
- Dimension order routing is deadlock free on k-ary n-arrays but not on tori with any $n \ge 1$.

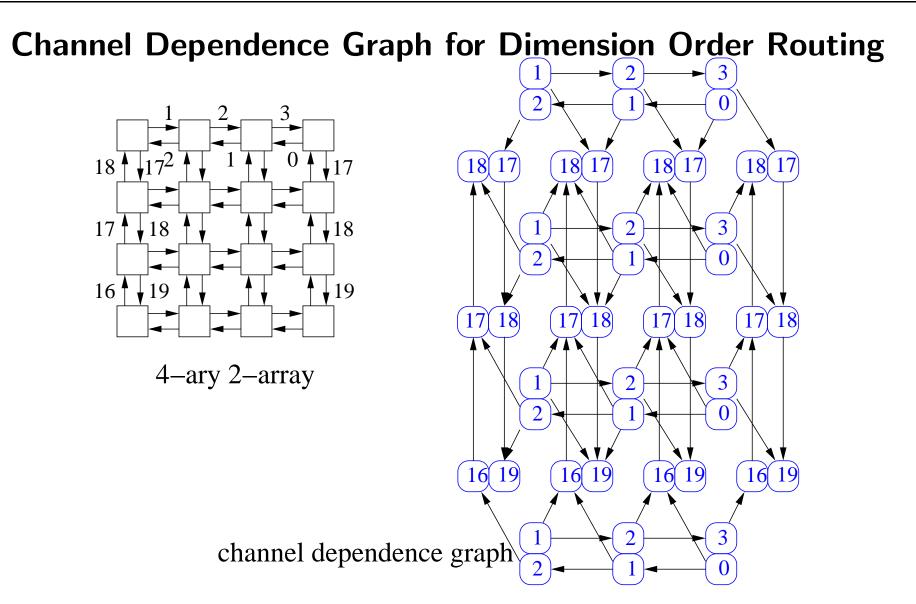


Deadlock in a 1-dimensional Torus



Message 1 from C-> B, 10 flits Message 2 from A-> D, 10 flits





Routing is deadlock free if the channel dependence graph has no cycles.

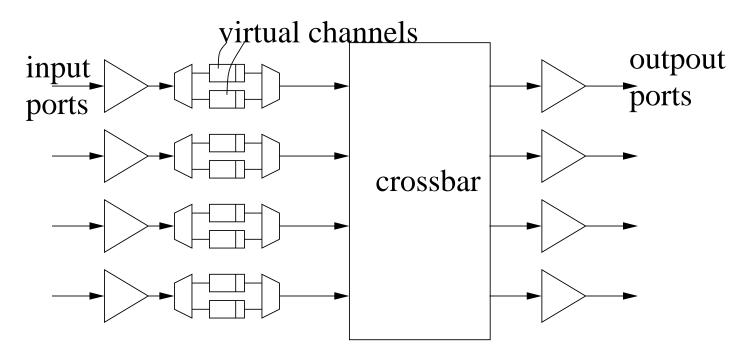


Deadlock-free Routing

- Two main approaches:
 - ★ Restrict the legal routes;
 - ★ Restrict how resources are allocated;
- Number the channel cleverly
- Construct the channel dependence graph
- Prove that all legal routes follow a strictly increasing path in the channel dependence graph.



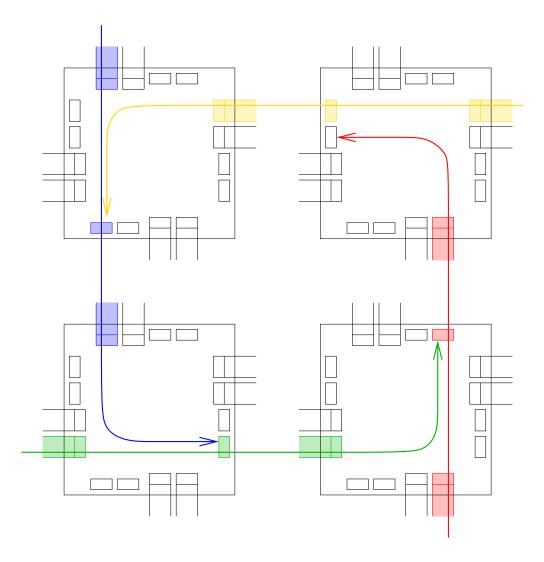
Virtual Channels



- Virtual channels can be used to break cycles in the dependence graph.
- E.g. all *n*-dimensional tori can be made deadlock free under dimension-order routing by assigning all wrap-around paths to a different virtual channel than other links.



Virtual Channels and Deadlocks

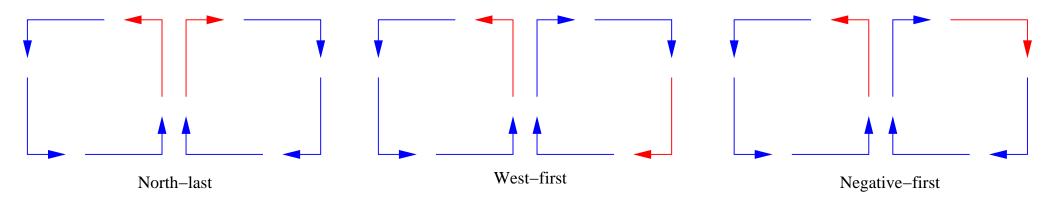




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Turn-Model Routing

What are the minimal routing restrictions to make routing deadlock free?



- Three minimal routing restriction schemes:
 - ★ North-last
 - ★ West-first
 - ★ Negative-first
- Allow complex, non-minimal adaptive routes.
- Unidirectional *k*-ary *n*-cubes still need virtual channels.



Adaptive Routing

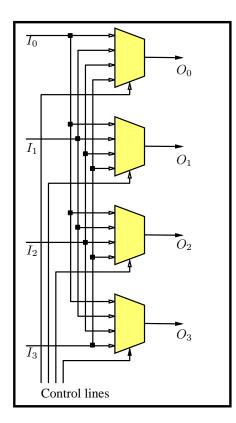
- The switch makes routing decisions based on the load.
- Fully adaptive routing allows all shortest paths.
- Partial adaptive routing allows only a subset of the shortest path.
- Non-minimal adaptive routing allows also non-minimal paths.
- Hot-potato routing is non-minimal adaptive routing without packet buffering.



Switch Design

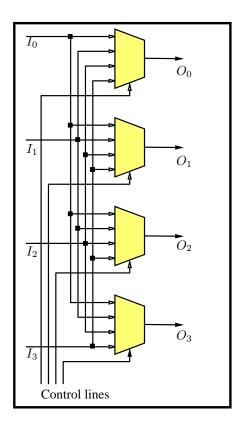


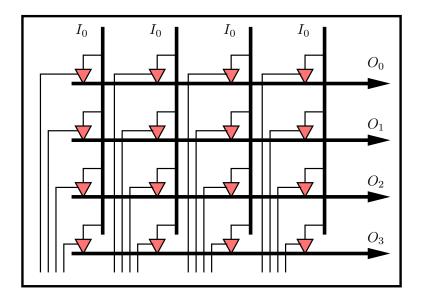
Switch Design





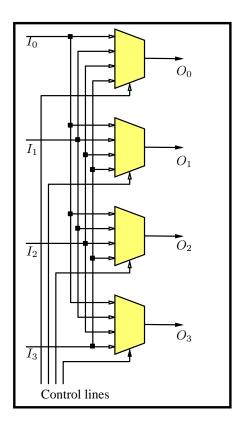
Switch Design

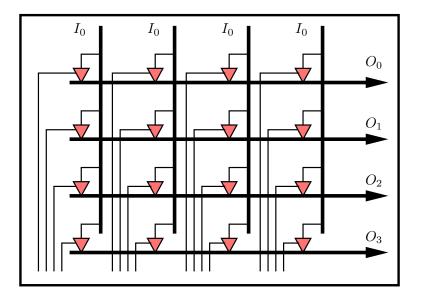


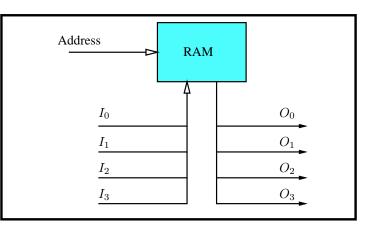




Switch Design









Switch Scaling

• Switches are wire dominated



Switch Scaling

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- Scaling with equal switch size by a factor s:
 - \star number of transistors: s^2
 - \star number of I/O's: s
 - \star speed of transistor: 1/s
 - \star speed of wires: 1
 - \star delay of the switch: 1



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- Scaling with equal I/O number by factor s:
 - \star size of the switch: $1/s^2$
 - \star speed of transistor: 1/s
 - \star speed of wires: 1/s



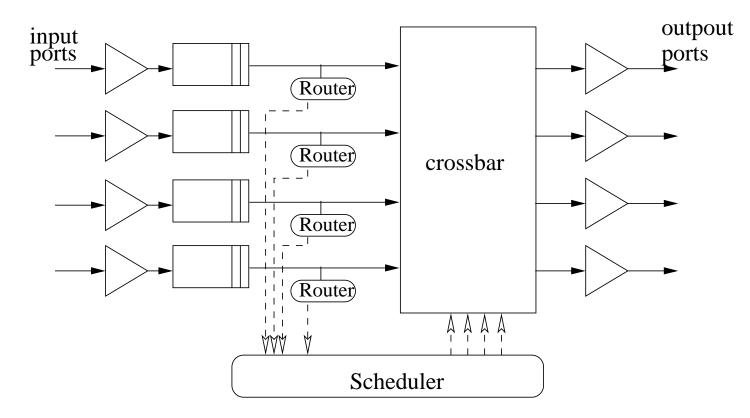
 \star delay of the switch: 1/s

Buffering

- Input buffering
- Output buffering
- Shared buffers
- Virtual channel buffers



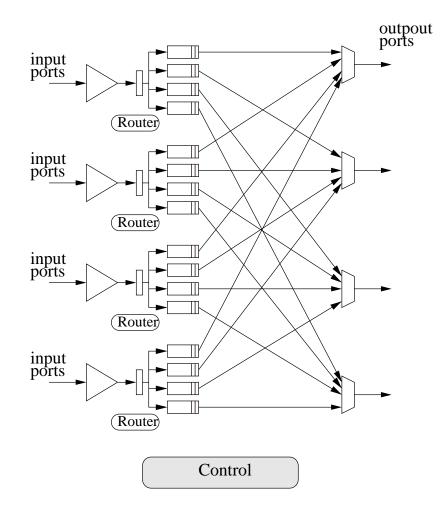
Input Buffering



Head-of line blocking limits output channel utilization to 60%.

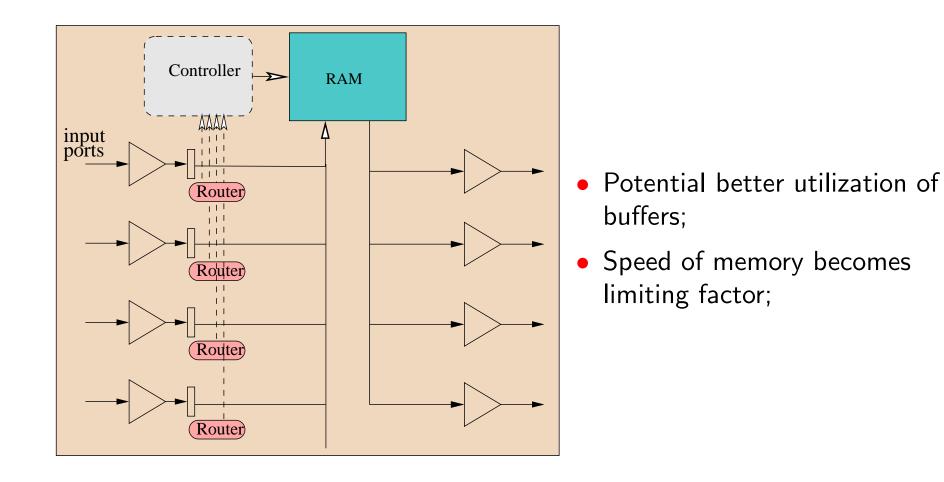


Output Buffering



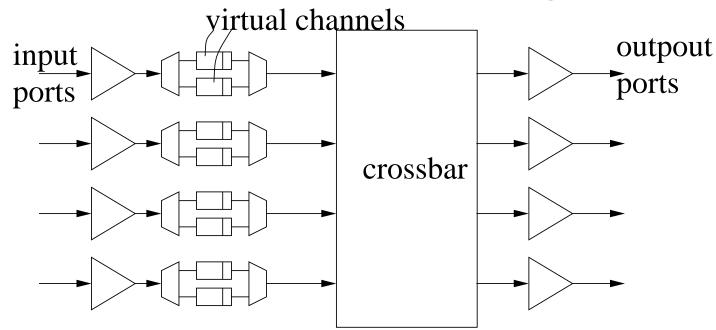


Shared Buffer Pool



VETENSKAP OCH KONST

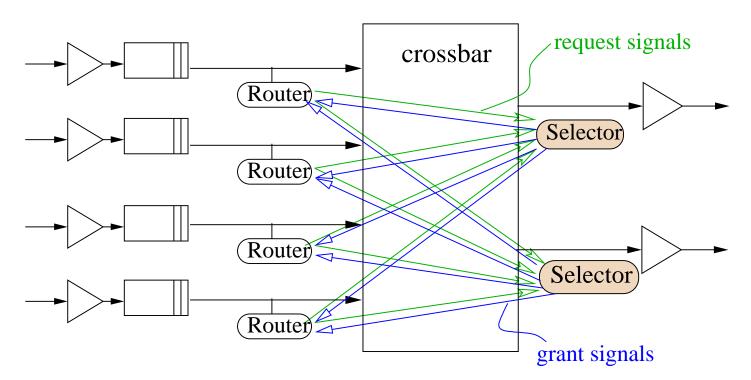
Virtual Channel Buffering



- Dynamic virtual channel allocation can
 - ★ increase buffer utilization,
 - ★ reduce head-of-line blocking.
- E.g. 256 nodes 2-ary butterfly with wormhole routing; 16 flits per link:
 - ★ no virtual channel: output channel saturation at 25% under random traffic;
 - \star 16 virtual channels: saturation at 80% traffic load;



Output Scheduling



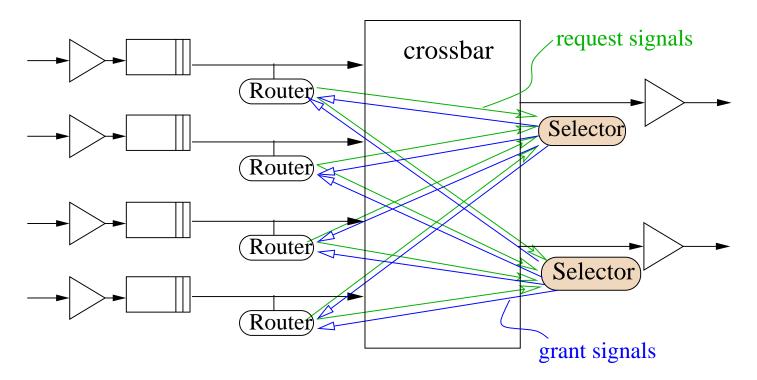
Output arbitration policy options:

Static priority Simple implementation; Potential for starvation; **Round-robin** requires additional state; **Random**

Oldest-first Same average latency as Random, but less variation;



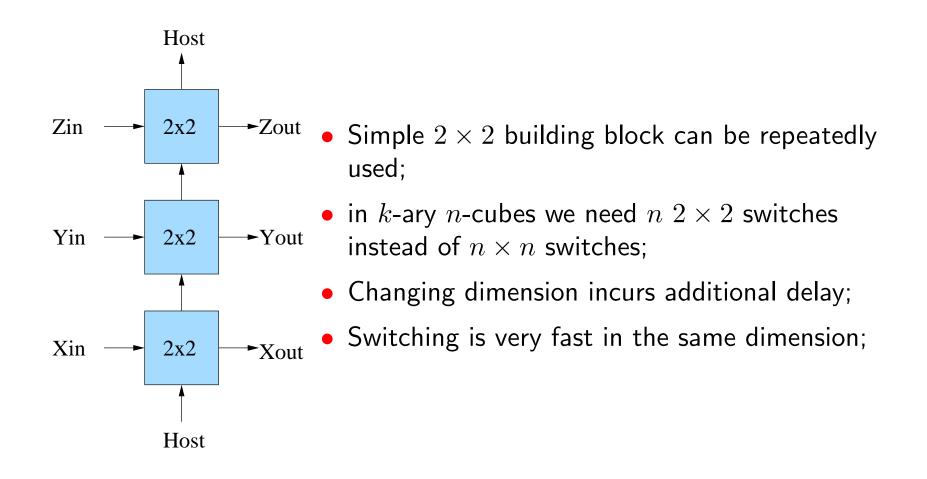
Output Scheduling and Routing Algorithms



- Restricted routing directions avoid full connectivity;
- Adaptive routing allows an input to request to several/all outputs



Stacked Dimension Switch





Flow Control

When a packet contends for a shared resource (link, buffer) we have three principle options:

- Buffering the packet and stalling new traffic;
- Dropping the packet;
- Allocating an alternative resource;



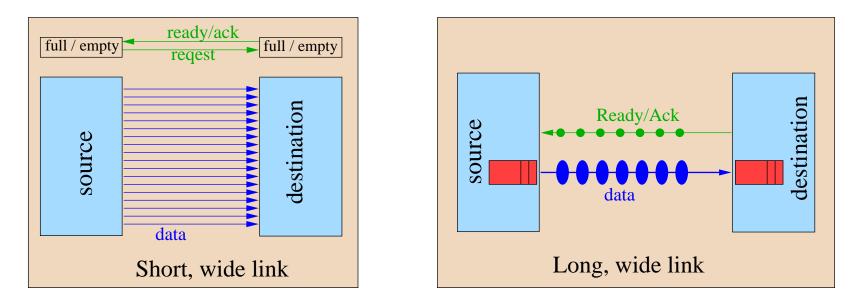
Flow Control

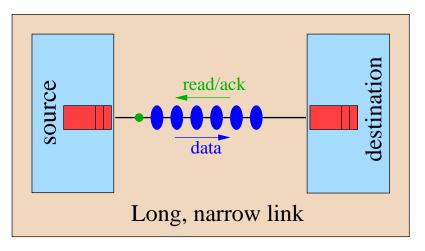
When a packet contends for a shared resource (link, buffer) we have three principle options:

- Buffering the packet and stalling new traffic;
- Dropping the packet;
- Allocating an alternative resource;
- Link level flow control;
- End to end flow controls;



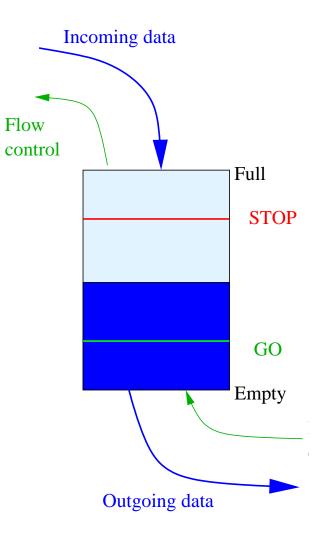
Link Level Flow Control







Flow Control with Watermarks



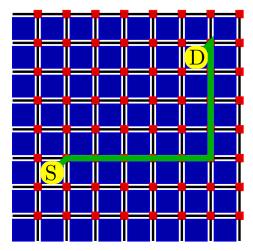


A. Jantsch, KTH

End-to-end Flow Control

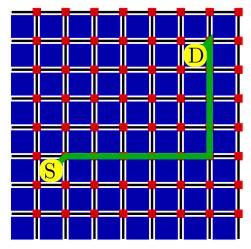
- Link level flow control can manage short term imbalances.
- Long term imbalances (more data is injected than drained) must be addressed with end-to-end flow control.



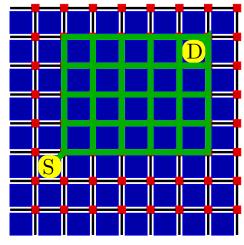


Deterministic Routing



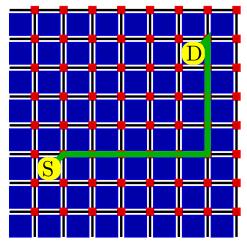


Deterministic Routing

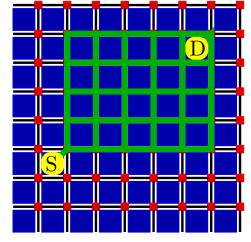


Minimal Adaptive Routing

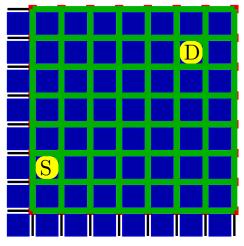




Deterministic Routing

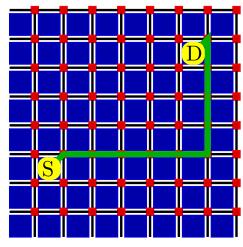


Minimal Adaptive Routing

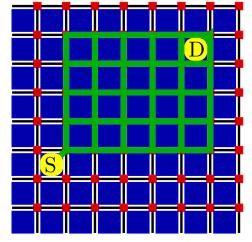


Nonminimal Adaptive Routing

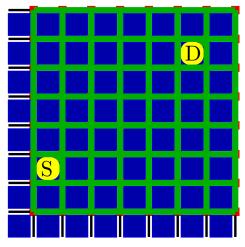




Deterministic Routing



Minimal Adaptive Routing



Nonminimal Adaptive Routing

Congestion causes:

- Source-destination imbalance;
- Hot spots;
- Random overload;



End-to-end Protocols and Admission Control

- Acknowledgement based protocols;
- Credit based protocols;
- Threshold based network admission protocols;



Summary

- Communication Performance: bandwidth, unloaded latency, loaded latency
- Organizational Structure: NI, switch, link
- Topologies: wire space and delay domination favors low dimension topologies;
- Routing: deterministic vs source based vs adaptive routing; deadlock;
- Switch: Buffering; output scheduling; flow control;
- Flow control: Link level and end-to-end control;



Issues beyond the Scope of this Lecture

- Power
- Clocking
- Faults and reliability
- Memory architecture and I/O
- Application specific communication patterns
- Services offered to applications; Quality of service



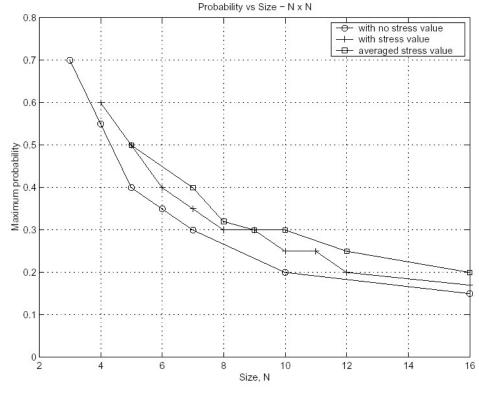
NoC Research Projects

- Nostrum at KTH
- Æthereal at Philips Research
- Proteo at Tampere University of Technology
- SPIN at UPMC/LIP6 in Paris
- XPipes at Bologna U
- Octagon at ST and UC San Diego



Nostrum (KTH)

- 2-d mesh topology
- Wide (128 bits), short links
- Non-minimal adaptive hot-potato routing
- No buffering
- Services: Best effort, guaranteed latency virtual circuits
- Four data protection levels at link layer



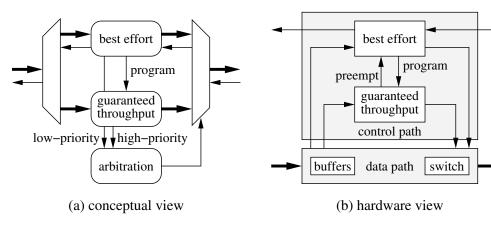
(from [Nilsson et al., 2003])



Æthereal (Philips)

- Topology: probably low dimensional tree or mesh, or dedicated
- Deterministic source based routing
- Wormhole or virtual cut-through switching
- Input buffering
- Selectable connection features:
 - ★ Integrity
 - \star Completion
 - ★ Ordering

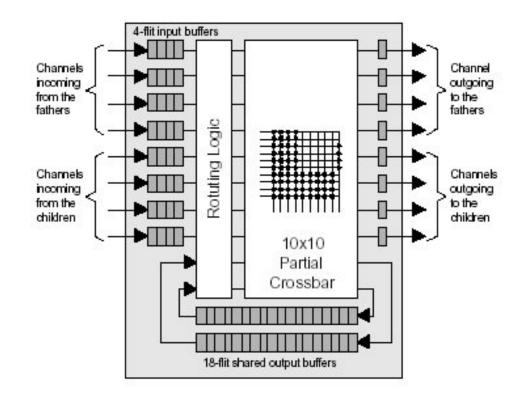
ETENSKA OCH KONST ★ Bounds on latency, throughput and jitter



(from [Goossens et al., 2003])

SPIN (UPMC/LIP6)

- Topology: Fat tree
- Wormhole switching
- Adaptive routing
- Input buffering
- Bidirectional 32 bit links
- Separate control network for configuration

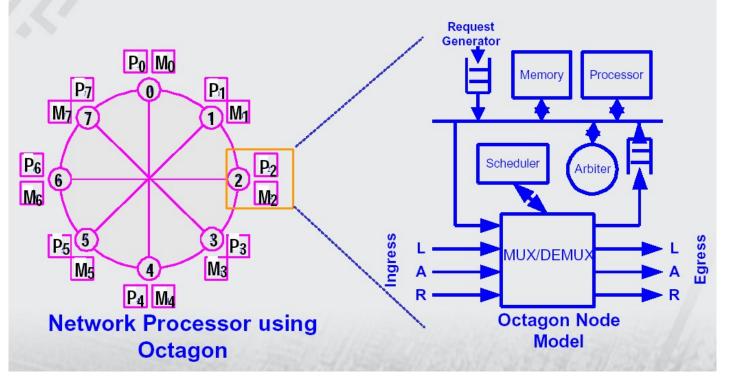


[Adriahantenaina et al., 2003]



Octagon (UCD, ST)

- Basic 8-node architecture
- Diameter: 2 hops
- Packet and circuit switching modes
- Source based routing with a 3 bit address in the header

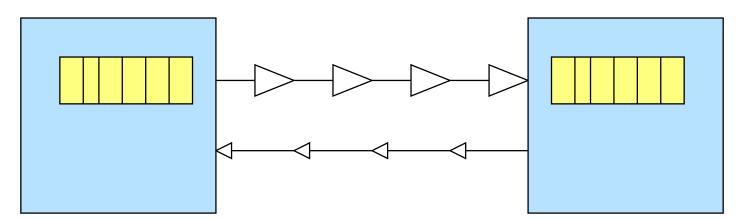


from [Karim et al., 2001]



XPipes (Bologna U)

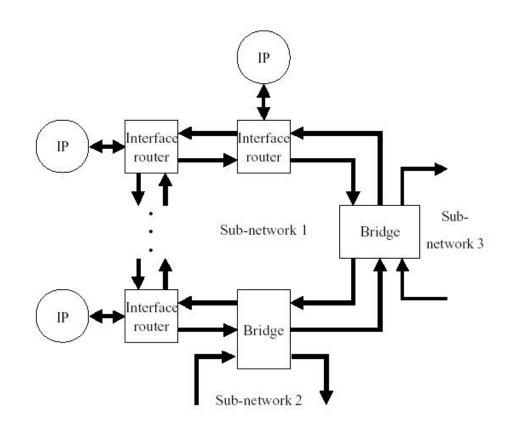
- Source based routing
- Wormhole switching
- Long, pipelined links
- Output buffering
- Virtual channels
- Acknowledgment based flow control with retransmission





Proteo (TUT)

- Objective is to develop a flexible library of communication IPs that support various topologies and routing strategies.
- Topology: Ring connecting local bus or star based clusters;
- Virtual cut-through switching
- Routing: Table based
- Buffering: Input and output buffering



(from [Alho and Nurmi, 2003])



To Probe Further - Books and Classic Papers

- [Agarwal, 1991] Agarwal, A. (1991). Limit on interconnection performance. *IEEE Transactions on Parallel and Distributed Systems*, 4(6):613–624.
- [Culler et al., 1999] Culler, D. E., Singh, J. P., and Gupta, A. (1999). *Parallel Computer Architecture - A Hardware/Software Approach*. Morgan Kaufman Publishers.
- [Dally, 1990] Dally, W. J. (1990). Performance analysis of k-ary n-cube interconnection networks. *IEEE Transactions on Computers*, 39(6):775– 785.
- [Duato et al., 1998] Duato, J., Yalamanchili, S., and Ni, L. (1998). Interconnection Networks - An Engineering Approach. Computer Society Press, Los Alamitos, California.
- [Leighton, 1992] Leighton, F. T. (1992). Introduction to Parallel Algorithms and Architectures. Morgan Kaufmann, San Francisco.



To Probe Further - NoC Examples

- [Adriahantenaina et al., 2003] Adriahantenaina, A., Charlery, H., Greiner, A., Mortiez, L., and Zeferino, C. A. (2003). SPIN: a scalable packet switched on-chip micronetwork. In *Proceedings of the Design Automation and Test Conference Designer's Forum*, pages 70–79.
- [Alho and Nurmi, 2003] Alho, M. and Nurmi, J. (2003). Implementation of interface router IP for Proteo network-on-chip. In *Proc. The 6th IEEE International Workshop on Design and Diagnostics of Electronics Circuits and Systems (DDECS'03)*, Poznan, Poland.
- [Goossens et al., 2003] Goossens, K., Dielissen, J., van Meerbergen, J., Poplavko, P., Rădulescu, A., Rijpkema, E., Waterlander, E., , and Wielage, P. (2003). Guaranteeing the quality of services in networks on chip. In Jantsch, A. and Tenhunen, H., editors, *Networks on Chip*, chapter 4, pages 61–82. Kluwer Academic Publishers.
- [Karim et al., 2001] Karim, F., Nguyen, A., Dey, S., and Rao, R. (2001). On-chip communication architecture for OC-768 network processors. In *Proceedings of the Design Automation Conference*, pages 678–683.
- [Nilsson et al., 2003] Nilsson, E., Millberg, M., Öberg, J., and Jantsch, A. (2003). Load distribution with the proximity congestion awareness in a network on chip. In Proceedings of the Design Automation and Test Europe (DATE), pages 1126–1127.

